

Transfer Functions of Switching Converters

Fast Analytical Techniques at Work with Small-Signal Analysis

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